Constructal design of Array of Tree-shaped Heat Sink

1R. Siddhardha, 2P. V. Vinay, 3M. Sumanth Sekhar
1Assistant Professor, 2Professor, 3Student
1,2Department of Mechanical Engineering,
GVP College for Degree and PG Courses, School of Engineering, Visakhapatnam, India
siddhardha93@gvpctedu.in, vpragada@gvpctedu.in, sunnysumant123@gmail.com.com

Abstract - An array of tree shaped heat sink is investigated and optimized by the constructal optimization method. In the first part of the paper a solid tree shaped heat sink was designed on the basis of conventional array of rectangular-fin heat sink, allocated volume as a constraint. In the second part, considering Fin material (volume fraction) as a constraint, an array of tree shaped heat sink with 3 stems was introduced. Experiments were conducted at constant heat input by varying Reynolds number from 15K to 40K, the center stem thickness (6mm) kept as constant and four different space to thickness ratios 1.5, 2, 2.75 and 4 (S/t) were considered for optimization.

Keywords - Tree-shaped Heat Sink, forced convection

1. INTRODUCTION

[1] Majed assumed a unidirectional conduction model with uniform heat transfer coefficient to analyze the thermal performance of the optimized tree-shaped fin by considering the space occupied, and material of the fin as constraints. The addition of more branches with equal length and thicknesses to the tree-shaped fin performs much better than longitudinal fin and the optimized T-shaped fins.[2] Bejan concentrated mainly on two aspects, the conductive and convective heat transfer over Constructal trees of circular fins. The geometry of the assembly is optimized to total volume, solid volume, number of circular fins, the external shape of the assembly, the optimal ratio of the central stem diameter to circular fin thickness, to minimize the thermal resistance and to maximize global conductance of the assembly. [3] They adopted triple optimization technique to optimize the constructal design i.e., Y-shaped assembly of fins, over the T-shaped structure by varying length ratio, thickness ratio of root to stem of Y-shaped fin and also the angle between a tributary branch and the horizontal. The objective is to minimize the global thermal resistance. [4] they analyzed the pressure drop and heat transfer characteristics of a tree-shaped micro channel net and proposed certain advantages over conventional parallel channel nets such as more uniform temperature distribution and better stability in case of accidental blockage. [5] Giulio compared the performances of finned (straight fins) surfaces, using (CFD) software, with the reference of Bejan’s Constructal theory and found a valid agreement. [6] "The larger the number of freedom degrees for evolving is, the more perfect the system performance is”. (XIE ZhiHui, 2010). They studied the heat transfer performance of the twice Y-shaped assemblies over T-shaped fin and Y-shaped fin and found the corresponding constructal optimization design has 36.37% decrease in thermal resistance when compare with other designs. [7] They optimized Umbrella-shaped assembly of cylindrical fins and defined dimensionless MTR(mean thermal resistance) based on EDR (entransy dissipation rate) with analytical method by considering the allocated space and fin-material volume as basic constraints. [8] the thermal and flow performances of heat sink systems are investigated numerically on several tree-shaped nets without/with loops. The tree-shaped nets with loops perform significantly better than nets without loops when the channel nets are blocked partially. [9] The heat conductance performance of the tree-shaped assembly becomes better as the fraction of fin material increases, thermal conductivity of fin grows smaller, and the heat transfer coefficient of fin over all the exposed surfaces becomes larger. [10] Optimized T-shaped assemblies of fins over cylindrical solid body with internal heat generation to enhance thermal performance. [11] Suggested that satisfying Biot number criterion is a better practice while designing optimal T-shaped heat sinks, to get feasible analytical solution. [12] The optimal design of Y-shaped fin heat sink, branched in the direction normal to fluid flow in a water cooled system decreases the thermal resistance up to 30% when compared with rectangular-fin heat sink. [13] Suggested Additive layer manufacturing (ALM) for complex designs. The heat transfer and fluid flow performance of the optimized heat sink is experimentally evaluated, and the results are compared with conventional heat sinks. [14] Genetic algorithm is used for geometrical optimization of morphing T-shaped fins attached to trapezoidal basement which enhances the performance by minimizes the thermal resistance under different area constraints. [15] Estimated the thermal performance of topology optimized heat sink to evaluate the thermal resistances, by providing optimum channel space using a numerical simulation, they found that the proxy model heat sink
has 15% lower thermal resistance and 26% smaller material mass compared to the conventional heat sink. [16] Proposed wavy micro channel heat sink with porous fins having rectangular cross-section which reduces pressure drop by 43.0–47.9%, while thermal resistance increases by 4.1–4.9%. the increase in channel length accelerates the cooling mixing by Dean Vortices and forced diffusion. [17] Concentrated to improve the thermal performance of heat sink by mitigating the heat transfer stagnation zone, to achieve this the corner part of the heat sink was removed and placed the heat sink in vertical position.[18] Introduce fork-shaped inserts for better thermal performance. In this paper, an array of tree shaped heat sink is investigated and optimized by the constructal optimization method. In the first part of this paper a solid tree shaped heat sink was designed on the basis of conventional array of rectangular-fin heat sink, volume as a constraint. In the second part, considering Fin material (volume fraction) as a constraint, an array of tree shaped heat sink with 3 branches was introduced. Experiments were conducted at constant heat input by varying inlet air velocities. Keeping the center array thickness (6mm) as constant, [9] The heat transfer enhancement occurs by adding material, by taking this as a consideration the array of tree shaped heat sink was optimized with four different space to thickness ratios 1.5, 2, 2.75 and 4 (S/t) respectively.

<table>
<thead>
<tr>
<th>Nomenclature</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Q</td>
<td>Rate of heat transfer (W)</td>
</tr>
<tr>
<td>h&lt;sub&gt;avg&lt;/sub&gt;</td>
<td>Average convective heat transfer coefficient (W/m&lt;sup&gt;2&lt;/sup&gt;K)</td>
</tr>
<tr>
<td>A&lt;sub&gt;t&lt;/sub&gt;</td>
<td>Total surface area (m&lt;sup&gt;2&lt;/sup&gt;)</td>
</tr>
<tr>
<td>T&lt;sub&gt;s&lt;/sub&gt;</td>
<td>Surface temperature (°C)</td>
</tr>
<tr>
<td>T&lt;sub&gt;out&lt;/sub&gt;</td>
<td>Outlet temperature (°C)</td>
</tr>
<tr>
<td>T&lt;sub&gt;in&lt;/sub&gt;</td>
<td>Inlet temperature (°C)</td>
</tr>
<tr>
<td>Nu</td>
<td>Nusselt number</td>
</tr>
<tr>
<td>K</td>
<td>Thermal conductivity (W/mK)</td>
</tr>
<tr>
<td>D&lt;sub&gt;h&lt;/sub&gt;</td>
<td>Hydraulic diameter (m)</td>
</tr>
<tr>
<td>U</td>
<td>Velocity (m/s)</td>
</tr>
<tr>
<td>Re</td>
<td>Reynolds number</td>
</tr>
<tr>
<td>ν</td>
<td>Kinematic viscosity</td>
</tr>
<tr>
<td>A&lt;sub&gt;c&lt;/sub&gt;</td>
<td>Cross sectional area (m&lt;sup&gt;2&lt;/sup&gt;)</td>
</tr>
<tr>
<td>P</td>
<td>Perimeter (m)</td>
</tr>
<tr>
<td>St</td>
<td>Stanton number</td>
</tr>
<tr>
<td>Pr</td>
<td>Prandtl number</td>
</tr>
<tr>
<td>Cf</td>
<td>Coefficient of friction</td>
</tr>
<tr>
<td>L</td>
<td>Length of the reference block (m)</td>
</tr>
<tr>
<td>B</td>
<td>Breadth of the reference block (m)</td>
</tr>
<tr>
<td>H</td>
<td>Height of the reference block (m)</td>
</tr>
</tbody>
</table>

2. MODEL

2.1. Array of rectangular fin heat sink

An array of rectangular-fin heat sink consists of 128 fins having 30mm length, 2.75 mm width, and 1.25 mm thickness over the base plate of thickness 4mm and area 36mmx 66mm made of Aluminium 6061 was taken from the CPU for reference. The volume occupied by the heat sink is 66mm x 36mm x 34mm.

2.2. Tree-shaped heat sink

A trunk of a tree acts like a bridge network to connect the roots and other parts of it by thick-walled cells to transfer water and nutrients. The basic idea of this model is to develop a heat sink which absorbs the heat from the source at the bottom and transfers to the branches through the trunk as shown in figure 1.

Fig.1: Constructal design
Table 1: Dimensions of space and thickness.

<table>
<thead>
<tr>
<th>Space (mm)</th>
<th>Thickness (mm)</th>
<th>S/t</th>
</tr>
</thead>
<tbody>
<tr>
<td>9</td>
<td>6</td>
<td>1.5</td>
</tr>
<tr>
<td>10</td>
<td>5</td>
<td>2</td>
</tr>
<tr>
<td>11</td>
<td>4</td>
<td>2.75</td>
</tr>
<tr>
<td>12</td>
<td>3</td>
<td>4</td>
</tr>
</tbody>
</table>

By considering the volume \((L \times B \times H)\) occupied by the reference model, a solid tree shaped heat sink was designed by Al-6061 as shown in Figure 3, to optimize the fin material, an array of tree shaped heat sink was introduced by varying space to thickness ratio in 4 stages. The dimensions of the tree shaped heat sink are as shown in Figure 2, and different space to thickness ratios are shown in Figure 2.

At 12mm space and 3mm thickness the model weighs same as reference heat sink. [9] As the tree-shaped assembly becomes better as the fraction of fin material increases. The thickness added in 1mm incremental in 4 stages up to 6mm by keeping the center stem thickness as constant.

2.3. Test sample preparation

In EDM the machining process is in the form of die-sinking machines and wire-cutting machines (Wire EDM). The designed tree shaped heat sink was made by wire EDM process in which material was removed by a slowly moving wire travels along a prescribed path of the work piece. by using electro-thermal mechanism. The material was removed in a sequence of discrete discharges between the wire electrode. The presence of dielectric fluid in the process creates a path for discharge as the fluid becomes ionized in the gap.

Fig. 2: Working models of (a) Array of rectangular fin heat sink, (b) Solid tree-shaped heat sink, (c) Array of tree-shaped heat sink
Fig. 3: Dimensions of different models (a) Array of rectangular fin heat sink, (b) Array of tree heat sink,

Fig. 4: 3D models of (a) Array of rectangular fin heat sink, (b) Solid tree-shaped heat sink, (c) Array of tree-shaped heat sink
2.4. Heat transfer and friction factor

The convective heat transfer rate $Q_{\text{conv}}$ from the electrically heated test surface is calculated using

\[ Q_{\text{conv}} = Q_{\text{electric}} - Q_{\text{cond}} \] (1)

Where $Q$ indicates the rate of heat transfer in which subscripts represent the convection, electrical, and conduction, respectively. The electrical heat input is calculated from the electrical potential and current supplied to the base plate. The conductive heat losses through the sidewalls can be neglected in comparison to those through the bottom surface of the test section. Using these findings, together with the facts that the two side walls and the top wall of the test section were well insulated and the readings of the thermocouple placed at the outer surface of the heating section were nearly equal to the ambient temperature.

The heat transfer from the test section by convection can be expressed as

\[ Q_{\text{conv}} = h_{\text{avg}} A_s \left[ T_s - \frac{T_{\text{out}} + T_{\text{in}}}{2} \right] \] (2)

Hence, the average convective heat transfer coefficient $h_{\text{avg}}$ could be deduced via

\[ h_{\text{avg}} = \frac{Q_{\text{conv}}}{A_s \left[ T_s - \frac{T_{\text{out}} + T_{\text{in}}}{2} \right]} \] (3)

The total surface area is equal to the sum of the projected area of the base plate and surface area contribution from the pin fins.

Total surface area ($A_s$) = Projected area of the base plate + Total surface area contribution from the blocks

Nusselt number calculated based on the total surface area, will reflect the effects of the variation in the surface area as well as the disturbances in the flow due to the fins on the heat transfer, in this study, the heat transfer enhancement characteristics were determined by using $Nu$ and $Re$ based on.

\[ Nu = \frac{h_{\text{avg}}}{k} \] (4)

\[ Re = \frac{D_h U}{\nu} \] (5)

\[ D_h = \frac{4A_s}{P} \] (6)

Where $D_h$ is the hydraulic diameter of the duct, $A_s$ is the cross-sectional area and $P$ is the perimeter of the duct.

Reynolds’s analogy gives a relation between the momentum and heat transfer of the fluid flow. The dimensionless parameter Stanton number relates skin friction coefficient from Eqn. (8)

\[ St = \frac{Nu}{RePr} \] (7)

\[ St = \frac{C_f}{2} \] (8)

In all calculations, the values of the thermophysical properties of the air were obtained at the bulk mean temperature, which is $T_m = \frac{(T_{\text{in}} + T_{\text{out}})}{2}$.

3. EXPERIMENTAL SETUP

The experimental setup consisting of the main duct test section and tested heat sinks as shown in Fig. 1. The internal cross section of the duct is 250 mm width and 150 mm height. The hydraulic diameter is 0.1875 m. Total length of the channel was 2.8 m and the length of the test section is 400 mm positioned horizontally.

The heating unit is placed at the bottom of the test section mainly consisted of an electric heater the outside of the test section was covered with a layer of glass wool, asbestos, and wood to ensure good insulation against heat losses to the surroundings. The electric power input to the heater was controlled by a variac transformer to maintain the constant heat flux at the base plate of the heat sinks. The projected area of the heating element is 40 mm², heat sink compound was used between the heater and base of the heat sink to eliminate thermal contact resistance. Since the heat sink models are compact in size, digital probe type thermocouples are used to measure the temperatures at different locations over the heat sinks. 3 k-type thermocouples are placed at the bottom of the heat sink to measure the average base plate surface temperature. Set of 3 k-type thermocouples are placed at the entrance and exit of the duct to measure the air inlet and outlet temperatures. The mean inlet velocities of the air flow entering the test section were determined by using Digital Thermo-Anemometer, having range of 0-30 m/s, with accuracy ±5%, it could also measure the air temperature in the range of -10 to 50°C. After attaining steady state at a given heat input 30 W, the temperatures were recorded. The pressure drop across the test section was measured using static pressure taps having accuracy 1.5%. They were located at upstream and downstream ends of the test section.

4. RESULT DISCUSSIONS

Fig 6: Temperature distribution of (a) Array of rectangular fin heat-sink, (b) Solid tree-shaped heat-sink, (c) Array of tree-shaped heat-sink
The Fig. 6 represents the temperature variation along the heat sinks using FLUENT CFD solver. Here the sink receives heat from the chip which is placed at the bottom, located at the center of cross sectional area 30mmx30mm. So more temperature is observed at the bottom of the sink i.e. at the base plate. As shown in Figure 6(a) the temperature distribution is uniform for all fins. Fins localized at the center conduct a better amount of heat, where as in Figure 6(b) and 6(c) shows the importance of trunk part to distribute the temperature to the tips of the branches from the base. The difference in solid tree shaped heat sink to array of tree shaped heat sink is the former design fails to convect the heat from the center trunk to surroundings. But the later one distributes more uniformly without accumulating the heat.

Fig. 7 shows Heat transfer co-efficient as a function of the Reynolds number based on hydraulic diameter, for different S/t ratios. As the velocity of the incoming air increases from 1.5m/s to 3m/s, as the Reynolds number increases the heat transfer coefficient also increases linearly, while considering different models, it was found that, at S/t ratio 2, i.e., 10mm space and 5mm stem thickness the thermal performance is significantly more than any other model. As mentioned earlier the tree-shaped assembly becomes better as the fraction of fin material increase it is also observed that the further increase in thickness contributes the rise internal thermal resistance to the heat sink and the trend is continued up to S/t is 0,i.e.,complete solid tree shaped heat sink. The trend of Nu number follows the same pattern as heat transfer coefficient with respect to Reynolds number in figure 8(b) and there is no much variation in coefficient of friction with different air velocities can be shown in Fig. 7(c).

5. CONCLUSION
An array of tree shaped heat sink was investigated and optimized by the constructal optimization method. Fin material (volume fraction) as a constraint, an array of tree shaped heat sink with 3 stems was introduced. Experiments were conducted at constant heat input by varying Reynolds number, by keeping the center array thickness (6mm) as constant,though four different space to thickness ratios 1.5,2,2.75 and 4 (S/t),were considered, at 2 the thermal performance is significantly more.
REFERENCES


