

Minimizing Makespan in Flow Shop under Continuous Machine Operation

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Abstract- The role of production scheduling is indispensable in the environment of manufacturing and service industries. Continuous machine operation or No-idle time on machines refers to the environment of production scheduling in which the machines once started work continuously to process all the jobs from first to last. The classical problem in flow shop scheduling is the minimization of makespan under different environments. The problem of makespan minimization in flow shop scheduling under continuous machine operation or no-idle situation is NP-hard. The heuristic proposed in this paper works on the principle of basic insertion to solve the flow shop problem for processing n -jobs on m -machines with continuous machine operation. The proposed constructive heuristic is compared with important heuristics solving no-idle problem that exists in flow shop literature. The computational result on Taillard's benchmark problems shows the superiority of the heuristic proposed over other heuristics.

Keywords- Flow shop; scheduling; constructive heuristic; no-idle.

1. INTRODUCTION

Production scheduling plays a vital role in manufacturing and service industries. For improving the production efficiency of the system, one must use effective and efficient solutions for manufacturing and scheduling technologies for the rapidly changing market demands having great competitive environment. According to the different industrial setups in flow shop, there prevail different constraints either on the jobs or on the machines to complete the task. The two important constraints in flow shop scheduling problem are No-wait of jobs and No-idle or Zero-idle time on machines. The No-wait flow shop scheduling problem (NWFSP) is an important branch of scheduling problems which related to 'zero buffer'. It arises due to the characteristics of jobs processing producing certain products, where the processing of jobs demands the processing to be continuous. The continuous flow shop originates in the scheduling theory because of the production environment in industry. In many flow shops, the production environment is such that the delay in job processing between the subsequent machines is not allowed i.e. the assumption of infinite storage capacity between the machines in flow shop is no longer valid. For maintaining the continuous flow of job, the processing of jobs is delayed on the first machine so that the jobs do not wait in the subsequent processing on machines. Various applications can be found in the industry related to this type of flow shop. For example, the

process of making iron sheets in industry involves the no-wait situation as the sequence in which the jobs are processed after the heating of iron is to be continuous so that the temperature of heated iron falls within the permissible interval specified. This constraint is necessary for the defect free production of iron sheets and making the good quality product. Also, in food processing industry, the food is canned immediately after the food is prepared so that the food quality is maintained. However, to maintain freshness in the food the continuous flow in the sequence of jobs processing is maintained throughout the process. In contrast to no-wait, the no-idle situation in some production scheduling occurs if the operation of the machines is not permitted to interrupt once started as their interruption causes increase in cost or decreases the benefits. The reason for this is the expensive parts used in the operation of machines with cost depending upon the actual time of operating or the environment of the manufacturing system does not allow. Such type of scheduling problem is known as no-idle flow shop scheduling problem. The problem of no-idle time of machines in the scheduling literature is also referred to Continuous Machine Operation (CMO). To maintain the no-idle environment in flow shop, the machines needs to be delayed for processing the first job so that idle time on machines for job processing is reduced to zero from start of processing to completion of jobs. Clear examples are the steppers used in the production

of integrated circuits by means of photolithography. Other examples come from sectors where less expensive machinery is used but where machines cannot be easily stopped and restarted. Ceramic roller kilns, for example, consume a large quantity of natural gas when in operation. Idling is not an option because it takes several days to stop and to restart. Other such example includes the production of glass fiber. The temperature inside the furnace for molten made from glass is maintained at high temperature, the furnace once stopped halts the production as it takes time in days to retain that temperature [7].

Adiri and Pohoryles [1] was first to study the m -machine no-idle situation in flow shop and showed that the problem $F_2 / prmu / C_{max}$ can be referred as the problem $F_2 / prmu, no-idle / C_{max}$ i.e. these two problems are equivalent. The solution of this can be obtained by applying Johnson [6] algorithm. For details relating to permutation ($prmu$) flow shop, one may refer to Pinedo [17]. Narain and Bagga [12] also developed an algorithm based on branch and bound method for two stage flow shop scheduling problem with objective as total flow time under no-idle condition. The problem related to $F_3 / prmu, no-idle / C_{max}$ have been studied extensively some researchers. Baptiste and Hguny [3] gave a integer linear programming model for solving $F_m / prmu, no-idle / C_{max}$, and a corresponding branch and bound algorithm; also see Saadani et al. [21]. Saadani et al. [19] explains the environment of no-idle in a three-stage production of engine blocks in a foundry which includes the casting of sand moulds and sand cores. Narain and Bagga [2] formulated the three stage flow shop problem minimizing the total elapsed time with zero idle time on machines. He illustrated that it is not necessary that the sequence having minimum total elapsed time also possesses the same under no-idle constraint. They discussed the concept of sequencing in rental situations under specific rental policy. The idle time on the first machine is always zero as first machine is required only for the time equal to the sum of the processing time of all the jobs on it. Under the circumstances of scarcity of funds, the machines have to be taken on rent or hired in order to complete the assignments. Hiring of machines enable saving working capital, give option for having the equipment, and allow the up-gradation to new technology. Minimization of the total hiring cost of machines would be the criterion in these types of situations. In this direction, they did

some work and explored the area for solving this problem [14].

Kamburowski [9] identified the simple network representation of total elapsed time which efficiently solves the three machine flow shop problem under no-idle situation. Besides this, the results of three machine problem are extended to m -machine no-idle flow shop problem. Woollam [24] studied the problem of no-idle time of machines using various benchmark heuristics like NEH heuristic [15] when modified to no-idle problem and other heuristics known for makespan problems. Narain and Bagga [13] gave four algorithms using branch and bound technique to solve n -job, m -machine flow shop problem under no-idle situation with objective of minimizing total elapsed time in which processing time of jobs follow certain relationship. Corresponding to these algorithms, theorems have been proved to show when one should hire the machine on rent to minimize total rental cost of machines. Saadani et al. [20] presented the model of $F_m / prmu / C_{max}$ problem with travelling salesman approach by using the nearest insertion technique and implemented with the help of the solver. Kalczyński and Kamburowski [7] proposed a improved heuristic based on the Johnson algorithm which outperforms the heuristic of Saadani et al. [21] and the modified NEH for no-idle constraint. Apart from this heuristic, Kalczyński and Kamburowski [8] have discussed no-wait and no-idle flow shops scheduling with makespan criterion and found that makepan with no-idle constraint is not the increasing function of processing times of jobs. Goncharov and Sevastyanov [5] have given review and approximation on the flow shop problem with no-idle constraints. Ruiz et al. [18] studied the variant of the classical permutation flow shop problem with makespan criterion with no-idle constraint. Baraz and Mosheiov [4] proposed the improved greedy (IG) heuristic with an improvement step involving pairwise exchange of jobs. Makuchowski [11] shows the significant correlation between the two variants of NEH algorithm for makespan with no-idle and without no-idle constraint i.e. the algorithm used for solving problem without no-idle can be effectively used for no-idle problems. Recently, Xiaoxia, and Yunhong [25] proposed a probability based model for solving mixed no-idle permutation flowshop scheduling problem.

Since, with advent of time the problem $F_m / prmu, no-idle / C_{max}$ is also solved by using metaheuristics for getting high quality results. Various

papers such as Pan and Wang [16], Seido Nagano and Januário, [22], Zhou and Chen [27], Li et al. [10] and Yazdani and Naderi [26] used metaheuristics for solving $F_m / pmu, no-idle / C_{max}$. This describes the significance of proposing improved constructive heuristic algorithm for providing the good initial solution to various metaheuristics. This is in turn implies that results of the metaheuristics can be improve further by the proposed constructive heuristic. In this work, a constructive heuristic is proposed and is compared with two important heuristics namely the improved greedy (IG) and Kalczynski-Kamburowski (KK) heuristic on various Taillard [23] instances. The computational result on Taillard's instances shows the superiority of the proposed heuristic (PH) over both the heuristics. The rest of paper is organized as follows: the section two deals with problem formulation. Section three explains the proposed heuristic algorithm. In section four, the working of the proposed heuristic algorithm is explained. Section five reports the results along with analysis of the results obtained. At the end, we conclude the paper in section six followed by references.

2. PROBLEM FORMULATION

Let some job $i (1 \leq i \leq n)$ is to be scheduled on machine $j (1 \leq j \leq m)$ in the same technological order with criteria to be optimized as minimization of makespan under no-idle constraint i.e. C_{max} . The general assumptions under which the n -jobs are processed through m -machines are: Pre-emption of jobs is not permitted. All jobs and machines are available at the beginning of processing. The machines are available throughout the processing and never breakdown. Each job is processed through each of the machine once and only once. Each machine can perform only one task at a time. The setup times of jobs on machines are negligibly small and hence can be ignored or are included in the processing time of jobs.

Let $t_{i,j}$ be the time of processing of the job i on the machine j , $T_i = \sum_{j=1}^m t_{i,j}$ be the sum total of processing times corresponding to job i on m machines. For calculating the makespan of a schedule of n -jobs in a no-idle situation concerning flow shop, we have to first find the time of initiation of machines so that the machines start processing jobs without any idle time on them. Following this, we denote this initiation of machines by L_j , $j = \{1,2,3,\dots,m\}$.

Clearly, $L_1 = 0$. We calculate the initiation of machines denoted by L_j as follows:

$$L_j = L_{j-1} + \max_{1 \leq k \leq n} \left\{ \sum_{i=1}^k t_{i,(j-1)} - \sum_{i=1}^{k-1} t_{i,j} \right\}, j = \{2,3,\dots,m\}$$

After the calculation of values of L_j , the makespan C_{max} can obtained from the following equation as:

$$C_{max} = L_m + \sum_{i=1}^n t_{i,m}.$$

3. PROPOSED ALGORITHM

The steps formulated for algorithm concerning flow shop scheduling problem, processing n -jobs through m -machines with objective of minimizing makespan under no-idle constraint (C_{max}) are given below.

Step1. Find the sum total of the processing time T_i of every job $i (i=1,2,3,\dots,n)$ on the given m -machines by the expression: $T_i = \sum_{j=1}^m t_{i,j}$.

Step2. Exhibit the job list according to the decreasing values of T_i so obtained in step 1.

Step3. Take the first two jobs from the job list. Find the two-job partial sequence with minimum C_{max} out of the possible two job sequences. Select it as the current partial sequence. If there is a tie for C_{max} , select that two job sequence for further construction of jobs in which the first job is with lower index to break the tie.

Step4. Take the next job from the job list and insert in all possible positions of the partial sequence obtained in step 3. Find the partial sequence with minimum C_{max} . This is the current sequence for further construction of final sequence of jobs. Break the tie if any as per step 3.

Step5. Check if there is more than one job in the job list. If so, consider the next two jobs else go to step 4. Find the possible two-job partial schedule from these. Select the two-job partial sequence with minimum C_{max} . Generate all the sequences by inserting the two-job partial sequence at all possible locations of the partial sequence so obtained in step 4. Select the sequence with minimum C_{max} as the current sequence. Next the first job of the latest pair of jobs is inserted in the all the possible locations of the current sequence to generate the possible sequences. If the any of these sequences have better result, then record that sequence as the current sequence. Break the tie if any as per step 3.

Step6. Repeat the step 4 and 5, if more jobs are present in the job list otherwise stop. The steps are repeated until all the jobs are scheduled. The sequence

so obtained is the final best sequence with minimum C_{max} .

4. NUMERICAL ILLUSTRATION

Consider the following flow shop instance with number of jobs, $n = 5$:

Table 1. Flow shop instance

Job <i>i</i>	Machine <i>j</i>		
	Machine 1	Machine 2	Machine 3
1	94	47	95
2	43	10	31
3	90	69	77
4	47	22	31
5	76	89	2

As per the step 1, the sum total of the processing times for every job on the three machines is $T_1 = 236$, $T_2 = 84$, $T_3 = 236$, $T_4 = 100$, $T_5 = 167$. Following step 1, arrange all the 5 jobs in the order of decreasing values of T_i in the job list resulting in {1, 3, 5, 4, 2}. According to step 3, pick the first two jobs from the job list namely {1, 3}. The possible two job sequences resulting from {1, 3} are 1-3 and 3-1 with respective $C_{max} = 356$ and 356. Since, there is a tie for the selection of two job sequence for further construction of jobs. Therefore, picking the sequence 1-3 as per the step proposed to break the tie. This is the best current sequence. Now picking the next job 5 using step 4 and inserting it at all the possible locations of the current sequence generating the sequences 5-1-3, 1-5-3 and 1-3-5 having $C_{max} = 432$, 406 and 365 respectively. The best current sequence of jobs having minimum $C_{max} = 365$ is 1-3-5. Now, pick next two unscheduled jobs {4, 2} from the job list. Find the minimum C_{max} for the possible arrangement of {4, 2}. The $C_{max} = 152$ for the partial sequences 4-2 and 2-4. Therefore, inserting the partial two job sequence 4-2 as block in the current best partial sequence so obtained in the last step generating the sequences 4-2-1-3-5, 1-4-2-3-5, 1-3-4-2-5, 1-3-5-4-2 with $C_{max} = 460$, 485, 485, 433 respectively. The sequence 1-3-5-4-2 becomes the current best sequence with minimum makespan. Now, insert the first job {4} of the last job-block in the last best sequence to generate 4-1-3-5-2, 1-4-3-5-2, 1-3-4-5-2, 1-3-5-4-2 and 1-3-5-2-4 with $C_{max} = 443$, 452, 452, 433, 427. The job sequence 1-3-5-4-2 retain as the best sequence. Further the second job 2 of the last pair is selected for inserting at all the possible locations of the current sequence generating the sequences 2-1-3-5-4, 1-2-3-5-4, 1-3-2-5-4, 1-3-5-2-4

and 1-3-5-4-2 with $C_{max} = 445$, 460, 460, 427 and 433 respectively. The sequence 1-3-5-2-4 is the final best sequence with minimum $C_{max} = 427$.

5. COMPUTATIONAL RESULTS

IG (improved greedy) is a heuristic method put forward by Baraz and Mosheiov [4] for solving NFSP. Their numerical tests showed that the IG heuristic method performed better. KK is a heuristic developed by Kalczyński and Kamburowski [7] showed that the KK heuristic performed better than NEH when modified to no-idle (NEH_M) problem. For the performance evaluation, the proposed heuristic (PH) is tested against the IG, KK heuristic and the results are compared to the solution produced by modified NEH for no-idle (NEH_M) on 100-Taillard instances. These 100-Taillard's instances contain 10-subsets having 10-problems each.

Table 2. Makespan values for 20, 50-job Taillard instances

Problem Instances	Makespan		Problem Instances	Makespan	
	NEH_M	PH		NEH_M	PH
20x5			50x5		
Ta001	1413	1408	Ta031	3028	3038
Ta002	1456	1432	Ta032	3172	3160
Ta003	1278	1294	Ta033	2876	2841
Ta004	1396	1402	Ta034	3107	3057
Ta005	1454	1463	Ta035	3158	3174
Ta006	1463	1469	Ta036	3061	3047
Ta007	1270	1295	Ta037	3120	3051
Ta008	1341	1301	Ta038	3040	3030
Ta009	1467	1417	Ta039	2700	2701
Ta010	1262	1230	Ta040	2885	2884
Avg	1380	1371	Avg	3014.7	2998.3
20x10			50x10		
Ta011	2266	2247	Ta041	3652	3528
Ta012	2198	2170	Ta042	3643	3639
Ta013	2007	2029	Ta043	3676	3556
Ta014	2048	1929	Ta044	3640	3755
Ta015	1799	1867	Ta045	3507	3507
Ta016	1835	1915	Ta046	4021	4023
Ta017	1988	1881	Ta047	3753	3702
Ta018	1931	1883	Ta048	4092	4082
Ta019	2054	2022	Ta049	3640	3585
Ta020	2011	1956	Ta050	3901	3867
Avg	2013.7	1989	Avg	3752.5	3724.4

		.9			
20x20			50x20		
Ta021	3482	3599	Ta051	5774	5898
Ta022	3329	3234	Ta052	6367	6378
Ta023	3578	3589	Ta053	5676	5671
Ta024	3227	3313	Ta054	5968	5995
Ta025	3433	3531	Ta055	5477	5503
Ta026	3677	3615	Ta056	6300	6146
Ta027	3584	3476	Ta057	5979	5969
Ta028	3372	3335	Ta058	5785	5766
Ta029	3480	3510	Ta059	5639	5628
Ta030	3855	3943	Ta060	5800	5859
Avg	3501.7	3514 .5	Avg	5876.5	5881.3

Table 3. Makespan values for 100, 200-job Taillard instances

Problem Instances	Makespan		Problem Instances	Makespan	
	NEH _M	PH		NEH _M	PH
100x5			100x20		
Ta061	5848	5893	Ta081	9694	9680
Ta062	5418	5418	Ta082	8820	8744
Ta063	5355	5403	Ta083	9308	9237
Ta064	5321	5333	Ta084	9619	9664
Ta065	5836	5836	Ta085	9869	9777
Ta066	5399	5383	Ta086	9049	9219
Ta067	5735	5743	Ta087	9111	9007
Ta068	5195	5204	Ta088	9005	9027
Ta069	5588	5621	Ta089	9498	9455
Ta070	5511	5477	Ta090	8825	8810
Avg	5520.6	5531 .1	Avg	9279.8	9262
100x10			200x10		
Ta071	6853	6849	Ta091	11840	11860
Ta072	6258	6189	Ta092	12560	12641
Ta073	6817	6756	Ta093	13341	13386
Ta074	6783	6629	Ta094	11844	11813
Ta075	6484	6527	Ta095	12197	12154
Ta076	6644	6658	Ta096	12015	12019
Ta077	6942	6956	Ta097	11735	11664
Ta078	7172	7176	Ta098	12397	12419
Ta079	7371	7232	Ta099	11191	11044
Ta080	7393	7429	Ta100	12624	12649
Avg	6871.7	6840 .1	Avg	12174. 4	12164 .9

Both proposed heuristic and modified NEH for no-idle (NEH_M) are implemented in MATLAB-R2008a. The average relative percent deviation

(ARPD) of the proposed heuristic (PH), IG and KK heuristic is calculated as the statistics for the performance measures.

Relative Percentage Deviation calculated as:

$$\text{Relative Percentage Deviation (RPD)} = \frac{\text{Makespan}_{\text{heuristic}} - \text{Makespan}_{\text{NEH}}}{\text{Makespan}_{\text{NEH}}} \times 100,$$

Where, $\text{Makespan}_{\text{heuristic}}$ is the value of the makespan obtained by the heuristic for a particular set of problems and $\text{Makespan}_{\text{NEH}}$ is the value of the makespan obtained from modified NEH for no-idle(NEH_M).

The ARPD results of proposed heuristic, IG [4] and KK heuristic [7] are compared and are shown in table 4. It can be observed that the proposed heuristic (PH) outperforms IG heuristic in all the 100-Taillard's instances considered. The proposed heuristic (PH) performs well than KK heuristic for job instances from 20x5 to 50x5 and for size 100x10 but KK features well for Taillard [23] problem instances of size 50x10 and larger except 100x10. For the overall average, it can be seen from table 4 that ARPD obtained by proposed heuristic (PH) algorithm is better than both IG and KK. That means that the makespan obtained by proposed heuristic (PH) algorithm is smaller than those by IG and KK.

Table 4. Comparison of IG, KK and Proposed Heuristic (PH)

Taillard problem instances	Average Relative Percentage Deviation		
	IG	KK	PH
20X5	9.19	0.87	-0.63
20X10	8.37	2	-1.18
20X20	5.4	1.29	0.37
50X5	11.53	-0.03	-0.54
50X10	12.34	-1.79	-0.75
50X20	12.44	-0.55	0.1
100X5	16.4	-0.24	0.19
100X10	13.98	0.08	-0.46
100X20	14.78	-2.57	-0.19
200X10	17.18	-0.55	-0.1
Overall Avg	12.16	-0.15	-0.32

6. CONCLUSION

In this paper, a constructive heuristic algorithm is proposed for solving no-idle flow shop scheduling problems. Under no-idle constraint the two more objective such as total flow time of jobs and mean flow time are also achieved as these problems

are equivalent under the no-idle constraint. The operational cost of the machines is also minimized as the machines are delayed in their operation and also they work continuously without waiting for any job. The proposed heuristic (PH) algorithm outperforms the two well known IG and KK heuristics existing in the literature on the 100-Taillard problem instances. The ARPD of the proposed heuristic (PH) is -0.32 as compared to the IG and KK heuristic with 12.16 and -0.15 respectively. The proposed heuristic (PH) algorithm therefore can be taken as the good initial solution to the various metaheuristics, thereby improving upon the solutions. The main aim is to provide a good initial solution to various algorithms based on the metaheuristics so that the results of these metaheuristics can be improved further.

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