Effect of Hall Currents and Non-Linear Density Temperature Variation on Convective Heat and Mass Transfer Flow of a Viscous Fluid past a Stretching Sheet with Thermo-Diffusion, Chemical Reaction and Heat Source

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Abstract:In this Paper, we study the combined influence of chemical reaction, Hall currents and Soret effect on convective heat and mass transfer flow of a viscous electrically conducting fluid past a stretching sheet. The equations governing the flow of heat and mass transfer have been solved by Galerkin finite element analysis with three nodded line segments. The velocity, temperature and concentration have been analysed for different values of M, m, N, Sc and So. The rate of heat and mass transfer on the plate has been evaluated numerically for different variations.

Keywords: Hall Currents, Non-Linear Density Temperature, Heat and Mass Transfer, Stretching Sheet, Thermo-Diffusion, Chemical Reaction, Heat Source

1. INTRODUCTION

Laminar boundary layer behavior over a moving continuous and linearly stretching surface is a significant type of flow has considerable practical applications in engineering, electrochemistry (Chin [13], Gorla [20]) and polymer processing, (Griffith [21], Erickson et. al. [18]). For example, materials manufactured by extrusion process and heat treated materials traveling between a feed roll and a windup roll or on a conveyor belt possesses the characteristics of a moving continuous surface. The hydromagnetic flow and heat transfer problems have become important industrially. To be more specific, it may be pointed out that many metallurgical processes involve the cooling of continuous strips or filaments by drawing them through a quiescent fluid and that in the process of drawing, these strips are sometimes stretched. Mention may be made of drawing, annealing and tinning of copper wires. In all the cases the properties of the final product depend to a great extent on the rate of cooling. By drawing such strips in an electrically conducting fluid subjected to magnetic fluid, the rate of cooling can be controlled and a final product of desired characteristics can be achieved. Another interesting application of hydromagnetics to metallurgy lies in the purification of molten metals from nonmetallic inclusions by the application of a magnetic field. The study of heat and mass transfer is necessary for the determining the quantity of the final product. However, there are fluids, which react chemically with some other ingredients present in them. The effect of a chemical reaction on the flow past an impulsively started infinite vertical plate with uniform heat flux was studied by Das et.al. [16], Anderson et. al. [6], have studied the diffusion of a chemical reactive species from a linearly stretching sheet. Anjalidevi and Kandaswamy [7] have investigated the effect of a chemical reaction on the flow along a semi infinite horizontal plate in the presence of heat transfer. Anjalidevi and Kandaswamy

[8] have studied the effect of a chemical reaction on the flow in the presence of heat transfer and magnetic filed. Muthukumaraswamy and Ganesan [30] have analyzed the effect of a chemical reaction on the unsteady flow past on impulsively started semi-infinite vertical plate, which is subject to uniform heat flux. McLeod and Rajagopal [28] have investigated the uniqueness of the flow of a Navier Stoke's fluid due to a linear stretching boundary. Raptis et. al. [33], have studied the viscous flow over a non-linearly stretched sheet in the presence of a chemical reaction and magnetic field.

In 1961, Sakiadis [36] who developed a numerical solution for the boundary layer flow field over a continuous solid surface moving with constant speed. Due to entertainment of ambient fluid, this boundary layer flow situation is quite different from the classical blasius problem over a semi-infinite flat plate. Suction or injection of a stretched surface was studied by Erickson et.al. [18], and Fox et.al. [19] for uniform velocity and temperature and investigates its effects on the heat and mass transfer in the boundary layer. Chen and Char [12] have studied the suction and injection on a linearly moving plate subject to uniform wall temperature and heat flux and the more general case using a power law velocity and temperature distribution at the surface was studied by Ali [5]. Magyari et.al. [26] have reported analytical and computational solution when the surface moves with rapidly decreasing velocities using the self-similar method. In all the papers mentioned above the effect of buoyancy force was relaxed. The above investigations having a definite bearing on the problem of a Polymer sheet extruded continuously from a dye. It is usually assumed that the sheet is in extensible, but situations may arise in the polymer industry in which it is necessary to deal with a stretching plastic sheet, as noted by Crane [15]. The study of heat generation or absorption in moving fluids is important in the problems dealing with chemical reactions and these concerned with dissociating

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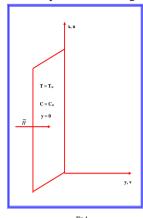
distribution. Consequently, the practice deposition rate in nuclear reactors, electronic chips and semi conductor waves. Vajravelu and Hadjinicolaou [42] have studied the heat characteristics in the laminar boundary layer of a viscous fluid over a stretching sheet with viscous dissipation or frictional heating and internal heat generation. Mohebujjaman et.al. [29] have studied the MHD heat transfer mixed convection flow along a vertical stretching sheet in presence of magnetic field with heat generation. Sajid et.al. [35] have discussed the non-similar analytic solution for MHD flow and heat transfer in a third-order fluid over a stretching sheet. Biliana et.al. [9] have analyzed the numerical solution of the boundary layer flow over an exponentially stretching sheet with thermal radiation. Jat et.al. [25] have studied the MHD flow and heat transfer over a stretching sheet.

The effect of chemical reaction on free convective flow and mass transfer of a viscous, incompressible and electrically conducting fluid over a stretching sheet was investigated by Afify [4] in the presence of a transverse magnetic field. In all these investigations the electrical conductivity of the fluid was assumed to be uniform. However, in an ionized fluid where the density is low and/or magnetic field is very strong, the conductivity normal to the magnetic field is reduced due to the spiraling of electrons and ions about the magnetic lines of force before collisions take place and a current induced in a direction normal to both the electric and magnetic fields. This phenomenon available in the literature is known as Hall Effect. Thus the study of MHD viscous flows, heat and mass transfer with Hall currents has important bearing in the engineering applications.

Hall effect on MHD boundary layer flow over a continues semi-infinite flat plate moving with a uniform velocity in its own plane in an incompressible viscous and electrically conducting fluid in the presence of a uniform transverse magnetic field were investigated by Watanabe and Pop [44]. Abo-Eldahab [1] have investigated free convective flows past a semi-infinite vertical plate with mass transfer. The effect of Hall current on the study MHD flow of an electrically conducting, incompressible Burger's fluid between two parallel electrically insulating infinite plane was studied by Rana et. al. [32].

Samadh et. al. [37] have studied MHD heat and mass transfer free convection flow along a vertical stretching sheet in the presence of magnetic field with heat generation. Seddeek [38] have studied the heat and mass transfer on a stretching sheet with a magnetic field in a visco-elastic fluid flow through a porous medium with heat source or sink. Veena et.al. [43] have discussed the non-similar solutions for heat and mass transfer flow in an electrically conducting visco-elastic fluid over a stretching sheet embedded in a porous medium. Hsiao has analysed the heat and mass transfer for electrical conducting mixed convection with radiation effect for visco-elastic fluid past a stretching sheet. Shit [39] has studied Hall effects on MHD free convective flow on mass transfer over a stretching

sheet. Raghavendra Rao [31] has discussed the effect of chemical reaction, Hall effects on the convective heat and mass transfer flow past a stretching sheet.



In all above studies the thermal -diffusion effect (Soret effect) has been neglected. This assumption is true when the concentration level is very low. There are, however, exemptions. The Soret effect for instance, has been utilized for isotope separation and in mixtures between gases with very low molecular weight (H2,He) and the medium molecular weight (N2,air) the Soret effect was found to be of a magnitude just it can not be neglected. (Eckert and Drake [17]). In view of the importance of this Soret effect, the free convection and mass transfer flow in an infinite vertical plate moving impulsively in its own plane, taking into the account of Soret effect. Abdul Sattar and Alam [2] have considered an unsteady convection and mass transfer flow of viscous incompressible fluid and electrically conducting fluid past a moving infinite vertical porous plate taking into the thermal diffusion effect. Similarity equations of momentum, energy and concentration equations are derived by introducing a time dependent length scale. Malsetty et al [27] studied the effect of both Soret and Dufour effects on the double diffusive convection with compensating horizontal and thermal and solute gradients. Ajay Kumar Singh[3] studied the study free convection and mass transfer flow with Hall Effect, viscous dissipation and joule heating, taking into account the thermal diffusion effect. Sreevani [41] has analyzed the free convective heat and mass transfer flow of a viscous incompressible fluid through a porous medium confined in vertical channel in the presence of constant heat source Q bounded by flat plates. Reddaiah et al [34] have discussed dissipative and Soret effect on convective heat and mass transfer through a porous medium in a vertical channel maintained at Non uniform temperature. Sreenivasa reddy [40] have discussed mixed convective heat and mass transfer through a porous medium in a channel with variable permeability and Soret effect. Reddaiah has considered finite element analysis of convective heat and mass

transfer through a porous medium in horizontal porous

channel with dissipative and Soret effects.

2. FORMULATION OF THE PROBLEM:

We consider the steady flow of an incompressible, viscous electrically conducting fluid past a flat surface which is assuming from a horizontal slit on a vertical surface and is stretched with a velocity proportional to distance from a fixed origin O. We choose a stationary frame of reference O(x,y,z) such that x-axis is along the direction of motion of the stretching surface, y-axis is normal to this surface and z-axis is transverse to the xy-plane. A uniform magnetic field in the presence of fluid flow induces the current $(J_x, 0, J_z)$.

When the strength of the magnetic field is very large we include the Hall current so that the generalized Ohm's law (Cowling[12]) is modified to

$$\overline{J} + \omega_e \tau_e \overline{J} x \overline{H} = \sigma(\overline{E} + \mu_e \overline{q} x \overline{H})$$
 (2.1)

where q is the velocity vector. H is the magnetic field intensity vector. \overline{E} is the electric field, \overline{j} is the current density vector, ω_e is the cyclotron frequency, τ_e is the electron collision time, σ is the fluid conductivity and μ_e is the magnetic permeability. The effect of Hall current give rise to a force in the z-direction which in turn produces a cross flow velocity in this direction and thus the flow becomes three –dimensional. To simplify the analysis, we assume that the flow quantities do not vary along z-direction and this will be valid if the surface is of very width along the z-direction. Neglecting the electron pressure gradient, ion-slip and thermo-electric effects and assuming the electric field E=0, equation (2.1) reduces

$$j_x - mH_0J_z = -\sigma\mu_e H_0 w \tag{2.2}$$

$$J_z + mH_0J_x = \sigma\mu_e H_0 u \tag{2.3}$$

where $m = \omega_{e} \tau_{e}$ is the Hall parameter.

On solving equations (2.2)&(2.3) we obtain

$$j_{x} = -\frac{\sigma \mu_{e}^{2} H_{0}^{2}}{1 + m^{2}} (mu - w)$$
 (2.4)

$$j_z = \frac{\sigma \mu_e^2 H_o^2}{1 + m^2} (u + mw)$$
 (2.5)

where u, w are the velocity components along x and z directions respectively,

The equation of Continuity is

$$\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} = 0 \tag{2.6}$$

The Momentum equations are

$$u\frac{\partial u}{\partial x} + v\frac{\partial u}{\partial z} = -\frac{\partial p}{\partial x} + v\frac{\partial^2 u}{\partial y^2} - \mu_e H_0 J_z - \rho \,\overline{g}$$
(2.7)

$$u\frac{\partial W}{\partial x} + v\frac{\partial W}{\partial y} = v\frac{\partial^2 W}{\partial y^2} + \mu_e H_0 J_x \qquad (2.8)$$

The energy equation is

$$\rho C_p \left(u \frac{\partial T}{\partial x} + w \frac{\partial T}{\partial z} \right) = k_f \frac{\partial^2 T}{\partial y^2} + Q(T - T_{\infty})$$
(2.9)

The diffusion equation is

$$(u\frac{\partial C}{\partial x} + v\frac{\partial C}{\partial y}) = D\frac{\partial^2 C}{\partial y^2} - k_0(C - C_{\infty}) + k_{11}\frac{\partial^2 C}{\partial y^2}$$
(2.10)

The equation of state is

$$\rho - \rho_0 = -\beta_0 (T - T_{\infty}) - \beta_1 (T - T_{\infty})^2 - \beta^{\bullet} (C - C_{\infty})$$
(2.11)

Substituting J_x and J_z from equations (2.4) & (2.5) in equations (2.7)&(2.8) we obtain

$$u\frac{\partial u}{\partial x} + v\frac{\partial u}{\partial y} = v\frac{\partial^{2} u}{\partial y^{2}} - \frac{\sigma\mu_{e}H_{0}^{2}}{1 + m^{2}} + \beta_{0}g(T - T_{\infty}) + \left| +\beta_{1}g(T - T_{\infty})^{2} + \beta^{\bullet}g(C - C_{\infty}) \right|$$
(2.12)

$$u\frac{\partial w}{\partial x} + v\frac{\partial w}{\partial y} = v\frac{\partial^2 w}{\partial y^2} + \frac{\sigma\mu_e^2 H_0^2}{1 + m^2} (m_0 u - w)$$
(2.13)

where T is the temperature and C is the concentration in the fluid. k_f is the thermal conductivity, Cp is the specific heat at constant pressure, $\beta_0 \& \beta_1$ is the coefficient of thermal expansion, β^{\bullet} is the volumetric expansion with concentration, Q_1^1 is the radiation absorption coefficient, q_r is the radiative heat flux, k_0 is the chemical reaction coefficient, D is the molecular viscosity, σ^* is the Stephen Boltzmann constant, β_R is the mean absorption coefficient.

The boundary conditions for this problem can be written as

$$u = bx, v = w = 0, T = T_w, C = C_w \text{ at } y = 0$$
 (2.17)

$$u = w = 0, T = T_{\infty}, C = C_{\infty} \text{ as } y \to \infty$$
 (2.18)

Where b>0. The boundary conditions on the velocity in (2.17) are the no-slip conditions at the surface at y=0, while the boundary conditions on the velocity as $y \to \infty$ follow from the fact that there is no flow far away from the stretching surface. The temperature and species concentration are maintained at a prescribed constant values T_w and C_w at the sheet and are assumed to vanish far away from the sheet.

On introducing the similarity variables

$$\eta = \sqrt{\frac{b}{v}}y, \qquad u = bx f'(\eta)
v = -\sqrt{bv} f(\eta) \qquad w = bx g(\eta)
\theta(\eta) = \frac{T - T_{\infty}}{T_{w} - T_{\infty}} \qquad \phi(\eta) = \frac{C - C_{\infty}}{C_{w} - C_{\infty}} \quad (2.19)$$

Equations (2.10), (2.12), (2.13) & (2.16) reduces to

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$$f''' + f f'' - f'^{2} + G(\theta + \gamma \theta^{2} + N\phi) - \frac{M^{2}}{1 + m^{2}} (f' + mg) = 0$$
(2.20)

$$g'' + fg' - (f' + \frac{M^2}{1 + m^2})g + \frac{mM^2}{1 + m^2}f' = 0$$

$$\theta'' + P f \theta^1 - \alpha \theta = 0 \tag{2.22}$$

$$\phi'' + Sc(\phi' f - \gamma \phi) = -\frac{ScSo}{N} \theta''$$
 (2.23)

and the boundary conditions (2.17)&(2.18) are now obtained from (2.19) as

$$f'(0) = 1$$
, $f(0) = 0$, $\theta(0) = \phi(0) = 0$ (2.24)
 $f'(\infty) = g(\infty) = \theta(\infty) = 0$ (2.25)

$$G = \frac{\beta g \left(T_w - T_\infty \right)}{h^2 x}$$
 (Grashof number),

$$M^{2} = \frac{\sigma \mu_{e}^{2} H_{0}^{2}}{bx}$$
 (Hartmann number)

$$N = \frac{\beta^* (C_w - C_\infty)}{\beta (T_w - T_\infty)}$$
 (Buoyancy

ratio),
$$So = \frac{k_{11}(T_w - T_\infty)}{b(C_w - C_\infty)\nu}$$
 (Soret parameter)

$$Sc = \frac{v}{D}$$
 (Schmidt number), $k = \frac{k_0}{b}$ (Chemical

reaction parameter)

For the computational purpose and without loss of generality ∞ has been fixed as 8.The whole domain is divided into 11 line elements of equal width, each element being three nodded.

3. FINITE ELEMENT ANALYSIS

The method basically involves the following steps:

- (1) Division of the domain into elements, called the finite element mesh.
- (2) Generation of the element equations using variational formulations.
- (3) Assembly of element equations as in step 2.
- (4) Imposition of boundary conditions to the equations obtained in step 3
- (5) Solution of the assumed algebraic equations.

The assumed equations can be solved by any of the numerical technique viz. Gaussian elimination, LU Decomposition method etc.

VARIATIONAL FORMULATION: The variational form associated with the equations(2.17)-(2.20)over a typical two nodded line at element(η_e, η_{e+1}) is given by

$$\int_{\eta_e}^{\eta_{e+1}} w_1(f'-h)d\eta = 0 \tag{3.1}$$

$$\int_{\eta_{e}}^{\eta_{e+1}} w_{12}(h'' + fh' - h^{2} + G(\theta + \gamma \theta^{2} + N\phi) - \frac{M^{2}}{1 + m^{2}}(h + mg)d\eta = 0$$
(3.2)

$$\int_{\eta_e}^{\eta_{e+1}} w_3(g'' + fg' - (h + \frac{M^2}{1 + m^2})g + \frac{mM^2}{1 + m^2}h)d\eta = 0$$
(3.3)

$$\int_{n}^{\eta_{e+1}} w_4(\theta'' + P f \theta' - \alpha \theta) d\eta = 0$$
 (3.4)

$$\int_{\eta_e}^{\eta_{e+1}} w_5(\phi'' + Sc(\phi'f - \gamma\phi) - \frac{ScSo}{N}\theta")d\eta = 0$$

Where w1, w2, w3, w4, w5 are arbitrary test functions and may be regarded as the variations in f, h, g, θ and ϕ respectively.

FINITE ELEMENT FORMULATION

The finite element method may be obtained from (3.1)-(3.5) by substituting finite element approximations of the form

$$f = \sum_{k=1}^{3} f_k \psi_k , h = \sum_{k=1}^{3} h_k \psi_k , g = \sum_{k=1}^{3} g_k \psi_k ,$$

$$\theta = \sum_{k=1}^{3} \theta_k \psi_k , \phi = \sum_{k=1}^{3} \phi_k \psi_k$$
(3.6)

We take w1=w2=w3=w4=w5= ψ_i^j (*i*, *j* = 1,2,3) (3.7) Using (3.7) we can write equations (3.1) - (3.5) as

$$\int_{\eta_{e}}^{\eta_{e+1}} \left(\frac{df}{d\eta} - h\right) \psi_{i}^{j} d\eta = 0$$

$$\int_{\eta_{e}}^{\eta_{e+1}} \left(\frac{d}{d\eta} \left(\frac{dh}{d\eta}\right) + f\left(\frac{dh}{d\eta}\right) - h^{2} + G(\theta + \gamma\theta^{2} + N\phi)\right)$$
(3.8)

$$-\frac{M^2}{1+m^2}(h+mg))\psi_i^j d\eta = 0$$

$$\int_{\eta_{e}}^{\eta_{e+1}} \frac{d}{d\eta} (\frac{dg}{d\eta}) + f(\frac{dg}{d\eta}) - (h + \frac{M^{2}}{1 + m^{2}})g$$

$$+ \frac{mM^{2}}{1 + m^{2}} h) \psi_{i}^{j} d\eta = 0$$

$$(3.10)$$

$$\int_{\eta_{e}}^{\eta_{e+1}} \left(\frac{d}{d\eta} \left(\frac{d\theta}{d\eta}\right) + Pf\left(\frac{d\theta}{d\eta}\right)\right) \psi_{i}^{j} d\eta - \alpha \int_{\eta_{e}}^{\eta_{e+1}} \theta \psi_{i}^{j} d\eta = 0$$
(3.11)

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$$\int_{\eta_{e}}^{\eta_{e+1}} \left(\frac{d}{d\eta} \left(\frac{d\phi}{d\eta} \right) + Sc\left(\left(\frac{d\phi}{d\eta} \right) f - \gamma \phi \right) - \frac{ScSo}{N} \frac{d}{d\eta} \left(\frac{d\theta}{d\eta} \right) \right) \psi_{i}^{j} d\eta = 0$$
(3.12)

Following Galerkine weighted residual method and integration by parts method the equations (3.8)-(3.12)

$$\int_{\eta_{e}}^{\eta_{e+1}} \left(\frac{df}{d\eta} - h \right) \psi_{i}^{j} d\eta = 0$$

$$\int_{\eta_{e}}^{\eta_{e+1}} \frac{d\psi_{i}^{j}}{d\eta} \left(\frac{dh}{d\eta} \right) d\eta - \int_{\eta_{e}}^{\eta_{e+1}} f \left(\frac{dh}{d\eta} \right) \psi_{i}^{j} d\eta + \int_{\eta_{e}}^{\eta_{e+1}} h^{2} \psi_{i}^{j} d\eta - G \int_{\eta_{e}}^{\eta_{e+1}} (\theta + \gamma \theta^{2} + N \phi) \psi_{i}^{j} d\eta + \int_{\eta_{e}}^{\eta_{e+1}} h^{2} \psi_{i}^{j} d\eta - G \int_{\eta_{e}}^{\eta_{e+1}} (\theta + \gamma \theta^{2} + N \phi) \psi_{i}^{j} d\eta + \int_{\eta_{e}}^{\eta_{e+1}} h^{2} \psi_{i}^{j} d\eta - G \int_{\eta_{e}}^{\eta_{e+1}} (\theta + \gamma \theta^{2} + N \phi) \psi_{i}^{j} d\eta + \int_{\eta_{e}}^{\eta_{e+1}} h^{2} \psi_{i}^{j} d\eta - G \int_{\eta_{e}}^{\eta_{e+1}} (\theta + \gamma \theta^{2} + N \phi) \psi_{i}^{j} d\eta + \int_{\eta_{e}}^{\eta_{e+1}} h^{2} \psi_{i}^{j} d\eta - G \int_{\eta_{e}}^{\eta_{e+1}} (\theta + \gamma \theta^{2} + N \phi) \psi_{i}^{j} d\eta + \int_{\eta_{e}}^{\eta_{e+1}} d\eta - G \int_{\eta_{e}}^{\eta_{e+1}} (\theta + \gamma \theta^{2} + N \phi) \psi_{i}^{j} d\eta + \int_{\eta_{e}}^{\eta_{e+1}} d\eta - G \int_{\eta_{e}}^{\eta_{e+1}} (\theta + \gamma \theta^{2} + N \phi) \psi_{i}^{j} d\eta + \int_{\eta_{e}}^{\eta_{e+1}} d\eta - G \int_{\eta_{e}}^{\eta_{e+1}} (\theta + \gamma \theta^{2} + N \phi) \psi_{i}^{j} d\eta + \int_{\eta_{e}}^{\eta_{e+1}} d\eta - G \int_{\eta_{e}}^{\eta_{e+1}} (\theta + \gamma \theta^{2} + N \phi) \psi_{i}^{j} d\eta + \int_{\eta_{e}}^{\eta_{e+1}} d\eta - G \int_{\eta_{e}}^{\eta_{e+1}} (\theta + \gamma \theta^{2} + N \phi) \psi_{i}^{j} d\eta + \int_{\eta_{e}}^{\eta_{e+1}} d\eta - G \int_{\eta_{e}}^{\eta_{e+1}} (\theta + \gamma \theta^{2} + N \phi) \psi_{i}^{j} d\eta + \int_{\eta_{e}}^{\eta_{e+1}} d\eta - G \int_{\eta_{e}}^{\eta_{e+1}} (\theta + \gamma \theta^{2} + N \phi) \psi_{i}^{j} d\eta + \int_{\eta_{e}}^{\eta_{e}} d\eta - G \int_{\eta_{e}}^{\eta_{e}} d\eta - G \int_{\eta_{e}}^{\eta_{e}} d\eta - G \int_{\eta_{e}}^{\eta_{e}} d\eta + \int_{\eta_{e}}^{\eta_{e}} d\eta - G \int_{\eta_{e$$

$$\begin{split} &\int_{\eta_{e}}^{\eta_{e+1}} \frac{d\psi_{i}^{j}}{d\eta} \frac{dg}{d\eta} d\eta - \int_{\eta_{e}}^{\eta_{e+1}} f\left(\frac{dg}{d\eta}\right) \psi_{i}^{j} d\eta \\ &+ \int_{\eta_{e}}^{\eta_{e+1}} ((h + \frac{M^{2}}{1 + m^{2}})g + \frac{mM^{2}}{1 + m^{2}} h) \; \psi_{i}^{j} d\eta = R_{1,j} + R_{2,j} \\ &where \\ &- R_{1,j} = \psi_{j}(\eta_{e}) \frac{dg}{d\eta}(\eta_{e}) \\ &R_{2,j} = \psi_{j}(\eta_{e+1}) \frac{dg}{d\eta}(\eta_{e+1}) \\ &\int_{\eta_{e}}^{\eta_{e+1}} (\frac{d\psi}{d\eta} \frac{d\theta}{d\eta} d\eta - P \int_{\eta_{e}}^{\eta_{e+1}} f\left(\frac{d\theta}{d\eta}\right)) \psi_{i}^{j} d\eta - Q_{1} N_{2} \\ &\int_{\eta_{e}}^{\eta_{e+1}} \phi \psi_{i}^{j} d\eta = S_{1,j} + S_{2,j} \\ &- S_{1,j} = \psi_{j}(\eta_{e}) \frac{d\theta}{d\eta}(\eta_{e}) \\ &S_{2,j} = \psi_{j}(\eta_{e+1}) \frac{d\theta}{d\eta}(\eta_{e+1}) \end{split}$$

(3.16)

$$\int_{\eta_{e}}^{\eta_{e+1}} \left(\frac{d\psi_{ij}^{j}}{d\eta} \frac{d\phi}{d\eta} - Sc \right)$$

$$\int_{\eta_{e}}^{\eta_{e+1}} \left(\left(\frac{d\phi}{d\eta} \right) f - \gamma \phi \right) \psi_{i}^{j} d\eta = T_{1,j} + T_{2,j}$$
(3.17)

 $-T_{1,j} = \psi_j(\eta_e) \frac{d\phi}{dn}(\eta_e) T_{2,j} = \psi_j(\eta_{e+1}) \frac{d\phi}{dn}(\eta_{e+1})$

Expressing $f^k, h^k, \theta^k, \phi^k$ in terms of local nodal values (3.14)-(3.17) we obtain

$$\int_{\eta_{e}}^{n_{e+1}} \sum_{k=1}^{3} h^{k} \int_{\eta_{e}}^{\eta_{e+1}} \frac{d\psi_{i}^{j}}{d\eta} (\frac{d\psi_{k}}{d\eta}) d\eta$$

$$- \sum_{k=1}^{3} f^{k} \int_{\eta_{e}}^{\eta_{e+1}} \psi^{k} (\frac{dh}{d\eta}) \psi_{i}^{j} d\eta$$

$$+ \sum_{k=1}^{3} (h^{k^{2}}) \int_{\eta_{e}}^{\eta_{e+1}} \psi_{k}^{k} 2 \psi_{i}^{j} d\eta - \frac{M^{2}}{1 + m^{2}}$$

$$- G \sum_{k=1}^{3} \int_{\eta_{e}}^{\eta_{e+1}} (\theta^{k} + N\phi^{k}) \psi_{k} \psi_{i}^{j} d\eta + \frac{M^{2}}{1 + m^{2}}$$

$$\sum_{k=1}^{3} \int_{\eta_{e}}^{\eta_{e+1}} (h^{k} + mg^{k}) \psi_{k} \psi_{i}^{j} d\eta = Q_{1,j} + Q_{2,j}$$
where
$$- Q_{1,jj} = \psi_{j} (\eta_{e}) (\frac{dh}{d\eta}) (\eta_{e})$$

$$Q_{21,jj} = \psi_{j} (\eta_{e+1e}) (\frac{dh}{d\eta}) (\eta_{e+1e})$$

$$\sum_{k=1}^{3} g^{k} \int_{\eta_{e}}^{\eta_{e+1}} \frac{d\psi_{i}^{j}}{d\eta} \frac{d\psi_{k}}{d\eta} d\eta$$

$$- \sum_{k=1}^{3} f^{k} g^{k} \int_{\eta_{e}}^{\eta_{e+1}} (\frac{d\psi_{k}}{d\eta}) \psi_{k} \psi_{i}^{j} d\eta$$

$$+ \sum_{k=1} \int_{\eta_{e}}^{\eta_{e+1}} ((h^{k} + \frac{M^{32}}{1 + m^{2}}) g^{k} + \frac{mM^{2}}{1 + m^{2}} h^{k})$$

$$\psi_{k} \psi_{i}^{j} d\eta = R_{1,j} + R_{2,j}$$
where
$$- R_{1,j} = \psi_{j} (\eta_{e}) \frac{dg}{d\eta} (\eta_{e})$$

$$R_{2,j} = \psi_{j} (\eta_{e+1}) \frac{dg}{d\eta} (\eta_{e+1})$$

(3.19)

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$$\sum_{k=1}^{3} \theta^{k} \int_{\eta_{e}}^{\eta_{e+1}} \left(\frac{d\psi}{d\eta} \frac{d\psi_{k}}{d\eta} d\eta - P \right)$$

$$\sum_{k=1}^{3} \int_{\eta_{e}}^{\eta_{e+1}} f^{k} \left(\frac{d\theta^{k}}{d\eta} \right) \psi_{k} \psi_{i}^{j} d\eta - Q_{1} N_{2}$$

$$\sum_{1}^{3} \int_{\eta_{e}}^{\eta_{e+1}} \phi^{k} \psi_{k} \psi_{i}^{j} d\eta = S_{1,j} + S_{2,j}$$

$$\text{where}$$

$$-S_{1,j} = \psi_{j} (\eta_{e}) \frac{d\theta}{d\eta} (\eta_{e}) k = 1$$

$$S_{2,j} = \psi_{j} (\eta_{e+1}) \frac{d\theta}{d\eta} (\eta_{e+1})$$

$$\sum_{k=1}^{3} \phi^{k} \int_{\eta_{e}}^{\eta_{e+1}} \left(\frac{d\psi_{ij}^{j}}{d\eta} \frac{d\psi_{k}}{d\eta} - Sc \right)$$

$$\sum_{k=1}^{3} \phi^{k} \int_{\eta_{e}}^{\eta_{e+1}} \left(\frac{d\psi_{ij}^{j}}{d\eta} \frac{d\psi_{k}}{d\eta} - \gamma \phi^{k} \right) \psi_{i}^{j} \psi_{k} d\eta - \frac{ScSo}{N}$$

$$\sum_{k=1}^{3} \theta^{k} \int_{\eta_{e}}^{\eta_{e+1}} \left(\frac{d\psi_{ij}^{j}}{d\eta} \frac{d\psi_{k}}{d\eta} d\eta = T_{1,j} + T_{2,j} \right)$$

$$\text{where}$$

$$-T_{1,j} = \psi_{j} (\eta_{e}) \left(\frac{d\phi}{d\eta} (\eta_{e}) - \frac{ScSo}{N} \frac{d\theta}{d\eta} (\eta_{e}) \right),$$

$$T_{2,j} = \psi_{j} (\eta_{e+1}) \left(\frac{d\phi}{d\eta} (\eta_{e+1}) - \frac{ScSo}{N} \frac{d\theta}{d\eta} (\eta_{e+1}) \right)$$

$$(3.21)$$

Choosing different ψ_{ij}^{j} corresponding to each element

 η_{e} in the equation (3.18) yields a local stiffness matrix of order 3x3 in the form

$$(f_{i,j}^{k})(u_{i}^{k}) - G(\theta_{i}^{k} + \gamma(\theta_{i}^{k})^{2} + NC_{i}^{k}) + \frac{M^{2}}{1 + m^{2}}(g_{i}^{k}) = (Q_{1,j}^{k}) + (Q_{2,j}^{k})$$
(3.22)

Likewise the equations (3.19),(3.20)&(3.21) give rise to a stiffness matrices

$$(g_{i,j}^{k}) + (f_{i}^{k}) - \frac{mM^{2}}{1 + m^{2}}(u_{i}^{k}) = (R_{1,j}^{k}) + (R_{2,j}^{k})$$

$$(3.23)$$

$$(e_{i,j}^{k})(\theta_{i}^{k}) - P(u_{i}^{k}) = (S_{1,j}^{k}) + (S_{2,j}^{k})$$

$$(3.24)$$

$$(l_{i,j}^{k})(\phi_{i}^{k}) - Sc(u_{i}^{k0})(\phi_{i}^{k})$$

$$- \frac{ScSo}{N}(m_{i,j}^{k})(\theta_{i}^{k}) = (T_{1,j}^{k}) + (T_{2,j}^{k})$$

$$\text{where } (f_{i,j}^{k}), (g_{i,j}^{k}), (\theta_{i,j}^{k}), (\phi_{i,j}^{k}), (e_{i,j}^{k}), (l_{i,j}^{k}),$$

$$(m_{i,j}^{k}) \text{ are } 3x3 \text{ matrices and}$$

$$(Q_{1,jj}^k), (Q_{2,jj}^k), (R_{1,jj}^k), (R_{1,jj}^k), (S_{1,ji}^k), (S_{1,ii}^k), (S_{1,ii}^k), (T_{1,ii}^k) and. (T_{1,ii}^k)$$

are 3x1 column matrices and such stiffness matrices (3.22)-(3.25) in terms of local nodes in each element are using inter element continuity assembled equilibrium conditions to obtain the coupled global matrices in terms of the global node values of h, f, g, θ and ϕ . In case we choose n quadratic elements then the global matrices are of order 2n+1. The ultimate coupled global matrices are solved to determine the unknown global values of velocity, temperature and concentration in the fluid region. In solving these matrices an iteration procedure has been adopted. The shape functions are

$$\psi_{i}^{i} = \frac{(y-8)(y-16)}{128}$$

$$\psi_{2}^{1} = \frac{(y-24)(y-32)}{128}$$

$$\psi_{3}^{1} = \frac{(y-40)(y-48)}{128}$$

$$\psi_{i}^{2i} = \frac{(y-4)(y-8)}{32}$$

$$\psi_{2}^{2i} = \frac{(y-12)(y-16)}{32}$$

$$\psi_{3}^{2} = \frac{(y-20)(y-24)}{128}$$

$$\psi_{i}^{3} = \frac{(3y-8)(3y-16)}{128}$$

$$\psi_{3}^{3} = \frac{(3y-24)(3y-32)}{128}$$

$$\psi_{3}^{4} = \frac{(y-2)(3y-4)}{8}$$

$$\psi_{4}^{4} = \frac{(y-2)(3y-4)}{8}$$

$$\psi_{4}^{4} = \frac{(y-6)(y-8)}{8}$$

$$\psi_{4}^{5} = \frac{(5y-8)(5y-16)}{128}$$

$$\psi_{5}^{5} = \frac{(5y-24)(5y-32)}{128}$$

$$\psi_{5}^{5} = \frac{(5y-40)(5y-48)}{128}$$
STIFFNESS MATRICES:

The global matrix for θ is The global matrix for ϕ is The global matrix for h is

 $A_3X_3=B_3$ $A_4X_4=B_4$ $A_5X_5=B_5$

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The global matrix for f is $A_6X_6=B_6$ The global matrix for g is $A_7X_7=B_7$

Particular Cases:

- **1.** In the absence of thermo-diffusion(So=0) the results are good agreeing with Raghavendra Rao [27].
- **2.** In the absence of thermal radiation $(N_1=0)$, thermodiffusion(So=0) the results are in agreeing with Shit [34].

5. DISCUSSION OF THE NUMERICAL RESULTS

We analyse the effect of chemical reaction, and thermo-diffusion on convective heat and mass transfer flow of a viscous, electrically conducting fluid past a stretching sheet. The non – linear coupled equations are solved by using a finite element technique with three nodded line segments.

The axial velocity $(f^{1}(\eta))$ is exhibited in figure 1 for different values of G. It is found that the axial velocity enhances with increase in thermal buoyancy parameter (G). From figs (2&3) we notice that the axial velocity depreciates with increase in the Hartman number M and enhances with Hall parameter (m). From fig.4 we find that lesser the molecular diffusivity smaller $|f^{l}(\eta)|$ in the flow region. With respect to buoyancy ratio N we find that when the molecular buoyancy force dominates over the thermal buoyancy force the magnitude of f^1 (η) enhances when the buoyancy forces act in the same direction and depreciates for the forces acting in opposite directions (fig.5). The variation of $f^1(\eta)$ with Eckert number Ec reveals that higher the dissipative heat larger $|f^{l}(\eta)|$ in the flow region (fig.6). An increase in the strength of the heat generating source reduces $|f^1(\eta)|$ (fig. 7). The variation of $f^{1}(\eta)$ with chemical reaction parameter k shows that $|f^{1}(\eta)|$ depreciates in the degenerating chemical reaction case and enhances in the generating chemical reaction cases (fig.8). Also higher the radiation absorption parameter Q_1 larger $|f^1(\eta)|$ in the region (fig.9). From fig.10 we find that $|f^1(\eta)|$ enhances with increase in the Soret parameter S₀. An increase in the density ratio γ enhances $|f^l(\eta)|$ (fig.11).

The transverse velocity $(f(\eta))$ is exhibited in figure 12 for different values of G. It is found that the transverse velocity experiences a depreciation with increase in $G \le 2X10^2$ and enhances with higher $G \ge$ 3X10². The variation of f with Hartmann number M shows that higher the Lorentz force lesser the transverse velocity (fig.13). An increase in the Hall parameter m \leq 1.5 results in an enhancement in f(η) and reduces with higher m=2 and again enhances with still higher m=2.5 (fig.14). With respect to Sc we find that lesser the molecular diffusivity smaller the transverse velocity (fig.15). When the molecular buoyancy force dominates over the thermal buoyancy force the transverse velocity enhances when the buoyancy forces act in the same direction while for the forces acting in opposite directions it depreciates in the flow region (fig.16). The variation of f with Ec is exhibited in fig.17. It is observed that higher the dissipative heat larger the transverse velocity. $f(\eta)$ reduces with increase in α (fig.

18). With respect to chemical reaction parameter k, we notice that the transverse velocity depreciates with k in the degenerating chemical reaction case and enhances in the generating chemical reaction case (fig.19). An increase in the radiation absorption parameter Q_1 results in an enhancement in $f(\eta)$ in the entire flow region (fig.20). An increase in S_0 enhances $|f(\eta)|$ (fig.21). From fig.22 we notice an enhancement in $|f(\eta)|$ with density ratio γ .

The cross velocity $(g(\eta))$ is exhibited in figure 23 for different values of G. It is found that |g| enhances with increase in G or M or m or Ec or Q_1 (figs.23,24,25,28 & 31). |g| reduces with increase in Sc (fig.26). |g| enhances with N>0 and reduces with |N| (fig.27). |g| reduces with the strength of the heat source (fig. 29). |g| experiences a depreciation with increase in the chemical reaction parameter k in the degenerating chemical reaction case and enhances in the generating chemical reaction case (fig.30). An increase in S_0 or γ enhances the $|g(\eta)|$ (figs.32 &33).

The non – dimensional temperature (θ) is shown in figure 34 for different values of G. We follow the convention that the non – dimensional temperature is positive or negative according as the actual temperature (T) is greater / lesser than Too. It is found that higher the thermal buoyancy parameter G or Hall parameter (m) or Soret Parameter (figs.34, 36 & 43) smaller the actual temperature. Higher the Lorentz force or lesser the molecular diffusivity larger the actual temperature (figs.35 & 37). When the molecular buoyancy force dominates over the thermal buoyancy force the actual temperature depreciates when the buoyancy forces act in the same direction and for the forces acting in opposite directions, it enhances in the flow region (fig.38). The variation of θ with Ec is exhibited in fig.39. It is observed that higher the dissipative heat larger the actual temperature. The actual temperature reduces with α (fig.40). The actual temperature enhances with increase in the chemical reaction parameter k>0 and reduces with |k| (<0) (fig.41). The actual temperature enhances with increase in radiation absorption parameter Q_1 in the entire flow region (fig. 42). From fig.44, the actual temperature reduces with γ.

The concentration distribution (ϕ) is shown in figure 45 for different values of G. We follow the convention that the non – dimensional concentration is positive or negative according as the actual concentration is greater / lesser than C∞. An increase in G or m or Sc or Ec or Q₁ leads to a depreciation in the actual concentration (figs.45,47,48, 50 & 53). Higher the Lorentz force larger the actual concentration (fig.46). When the molecular buoyancy force dominates over the thermal buoyancy force the actual concentration depreciates when the buoyancy forces act in the same direction and for the forces acting in opposite directions it enhances in the flow region (fig.49). The actual concentration enhances with α (fig.51). The actual concentration reduces with k>0 and enhances with k<0 (fig.52). Higher the thermal diffusion effect larger the concentration in the flow

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region (fig.54). The actual concentration reduces with γ (fig.55)

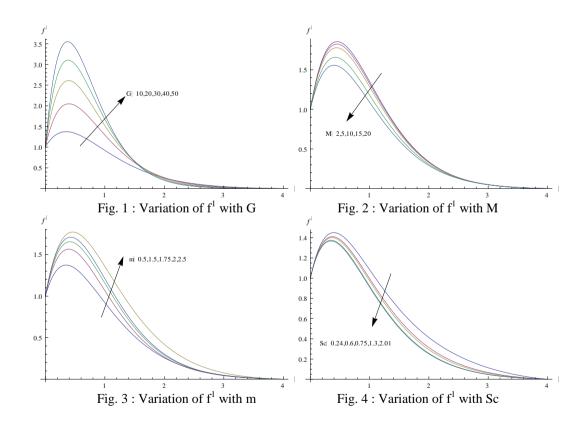
The stress component (τ_x) is shown in tables 1, 5 & 9 for different values. It is found that $|\tau_x|$ at $\eta=0$ enhances with increase in G or m and reduces with M. Lesser the molecular diffusivity smaller $|\tau_x|$. It enhances with increase in the buoyancy ratio N>0 and reduces with |N| (<0)| (table 1). $|\tau_x|$ depreciates with increase in the chemical reaction parameter k>0 and enhances in the generating case(k<0) and enhances with $|\Omega_1||\tau_x|$ reduces with increase in the strength of the heat generating source and enhances with that of heat absorbing source. An increase in Ec or S_0 or γ leads to an enhancement in $|\tau_x|$

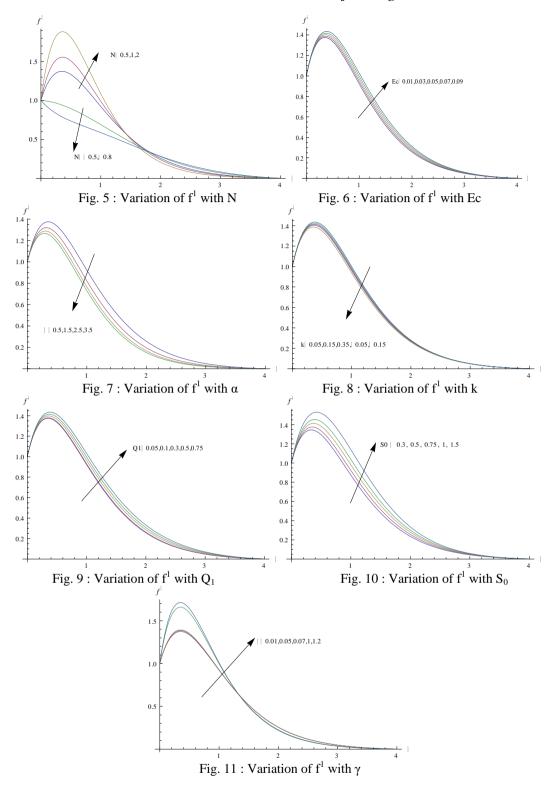
The stress component (τ_z) at $\eta=0$ is shown in tables 2, 6 & 10 for different values. $|\tau_z|$ enhances with increase in G or Q_1 or m or Ec or γ . An increase in Sc or heat source parameter $|\alpha|$ leads to a depreciation in $|\tau_z|$. It reduces with increase in the chemical reaction parameter k>0 and enhances with k<0. $|\tau_z|$ enhances with buoyancy ratio N>0 and reduces with |N|(<0) and also it enhances with S_0 or γ .

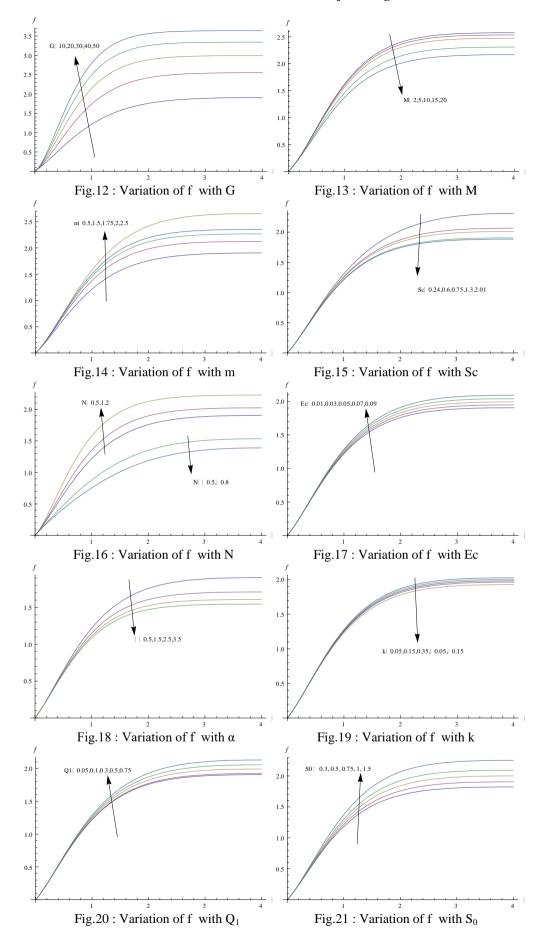
The rate of heat transfer (Nusselt number) at η = 0 is depicted in tables 3,7 &11. The rate of heat transfer enhances with increase in G or heat source

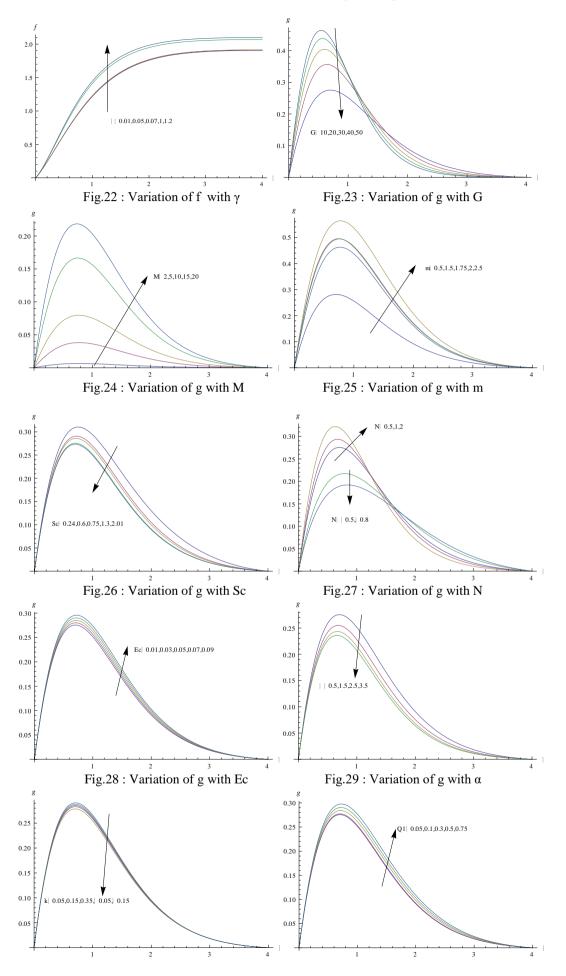
parameter α or Hall parameter m. |Nu| reduces with M or Q_1 or Ec or S_0 . With respect to buoyancy ratio N we find that |Nu| enhances with N>0 and reduces with |N| (<0). Also |Nu| depreciates in the degenerating chemical reaction case and enhances in the generating chemical reaction case. An increase in the density ratio γ leads to an enhancement in |Nu| at η =0.

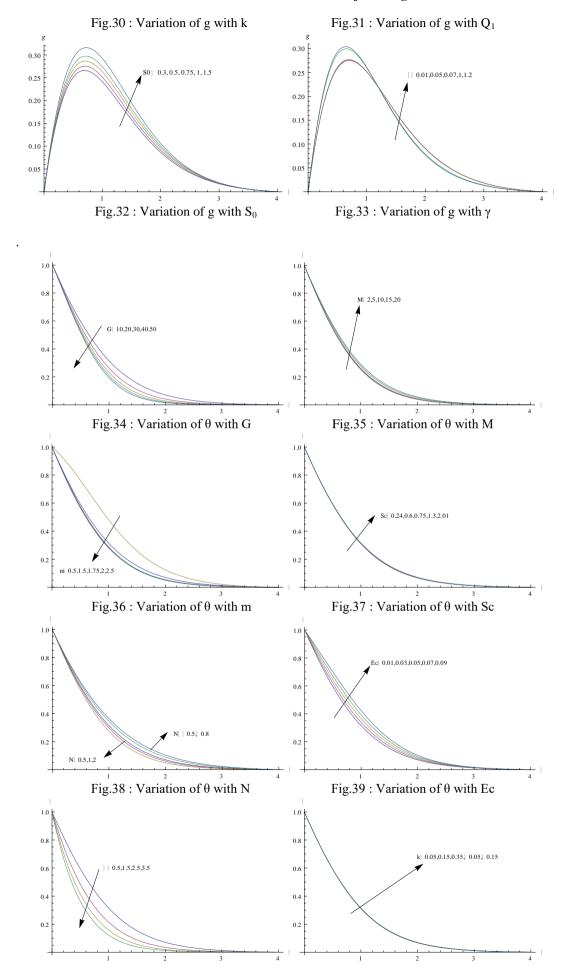
The rate of mass transfer (Sherwood number) at $\eta = 0$ is shown in tables 4,8&12 for different variations. It is found that higher the thermal buoyancy parameter G or Hall parameter m or lesser the molecular diffusivity larger |Sh| at $\eta = 0$. With respect to N, we find that |Sh| enhances with N > 0 when the buoyancy forces act in the same direction and depreciates with |N|(<0) when they act in opposite directions. Higher the Lorentz force lesser |Sh| at $\eta=0$. |Sh| experiences an enhancement in both degenerating and generating chemical reaction cases. Also it enhances with radiation absorption parameter Q₁ or Ec or γ. |Sh| reduces with increase in the strength of the heat generating source or enhances with that of heat absorbing source. |Sh| reduces with $S_0 \le 1.5$ and enhances with $S_0 \ge 2.5$. The variation of Sh with density ratio y shows that the non-linearity in the density temperature relation enhances |Sh| at $\eta=0$.

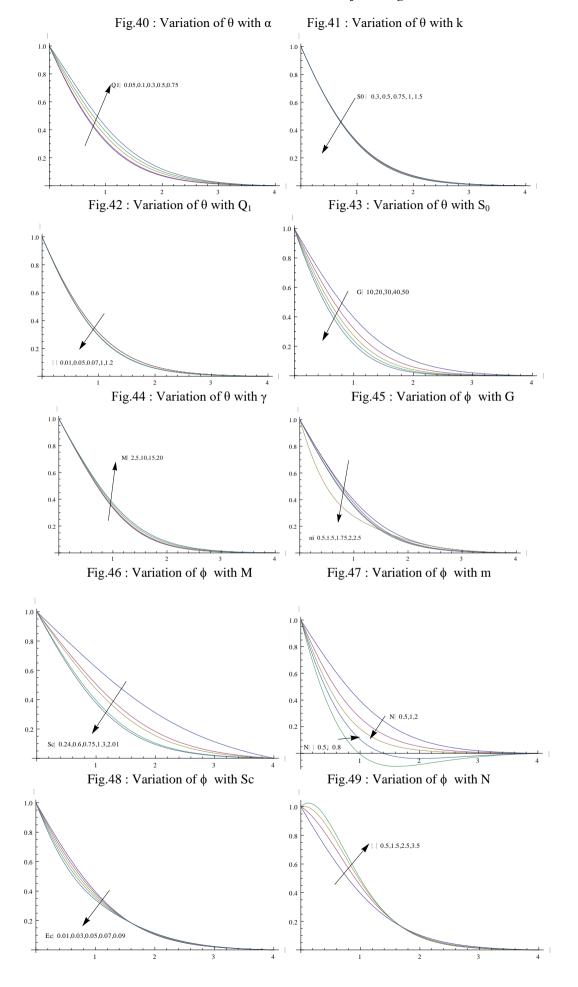




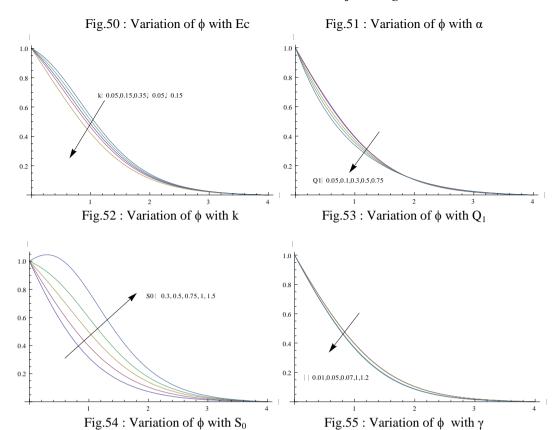








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Shit-2-stress τ_x (TABLE 1)

M	I	II	III	IV	V	VI	VII	VIII
1	4.42984	12.4133	6.86159	1.69482	0.792816	4.43329	4.80657	4.59493
3	4.41336	12.3945	6.84447	1.67907	0.777271	4.42711	4.78875	4.57801
5	4.38594	12.363	6.81598	1.65289	0.751426	4.41674	4.7591	4.54984
G	10	30	10	10	10	10	10	10
N	0.5(Sc=1.3)	0.5	1.5	-0.5	-0.8	m=1.5	Sc=0.22	0.6

 τ_z (TABLE 2)

M	I	II	III	IV	V	VI	VII	VIII
1	0.00429032	0.00536462	0.00458438	0.00385731	0.00368823	0.00495647	0.0046321	0.00441349
3	0.0170594	0.0213798	0.0182439	0.0153139	0.0146313	0.0197809	0.0184219	0.0175518
5	0.0380067	0.047812	0.0407015	0.03403	0.0324715	0.0443388	0.0410541	0.0391127
G	10	30	10	10	10	10	10	10
N	0.5(Sc=1.3)	0.5	1.5	-0.5	-0.8	m=1.5	Sc=0.22	0.6

Nu (TABLE 3)

M	I	II	III	IV	V	VI	VII	VIII
1	1.02339	1.09283	1.05588	0.987808	0.96247	1.0235	1.0381	1.0293
3	1.02244	1.09178	1.05494	0.986854	0.96149	1.02289	1.03704	1.02832
5	1.02088	1.09003	1.05338	0.985271	0.95986	1.02186	1.03528	1.02669
G	10	30	10	10	10	10	10	10
N	0.5(Sc=1.3)	0.5	1.5	-0.5	-0.8	m=1.5	Sc=0.22	0.6

Sh (TABLE 4)

M	I	II	III	IV	V	VI	VII	VIII
1	0.77875	1.05503	1.23885	1.85249	1.58967	0.778929	0.416396	0.593274
3	0.778278	1.05485	1.23818	1.85112	1.58837	0.778994	0.416145	0.59287
5	0.777487	1.05454	1.23706	1.84883	1.58621	0.779093	0.415725	0.592194
G	10	30	10	10	10	10	10	10
N	0.5(Sc=1.3)	0.5	1.5	-0.5	-0.8	m=1.5	Sc=0.22	0.6

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τ_x (TABLE 5)

M	I	II	III	IV	V	VI	VII	VIII	IX
1	4.42984	4.21331	4.06834	4.80561	5.71896	4.23541	4.10028	4.73696	5.27173
3	4.41336	4.19697	4.05218	4.78933	5.69989	4.21889	4.08382	4.72083	5.25682
5	4.38594	4.1698	4.0253	4.76225	5.66844	4.19142	4.05644	4.6942	5.23208
α	0.5	1.5	2.5	-0.5	-1.5	0.5	0.5	0.5	0.5
γ	0.5	0.5	0.5	0.5	0.5	1.5	2.5	-0.5	-1.5

τ_z (TABLE 6)

M	I	II	III	IV	V	VI	VII	VIII	IX
1	0.0042903	0.0041602	0.0040771	0.0045118	0.0034611	0.0042213	0.0041743	0.00439	0.0045718
	2	8	1	4	2	5	1	8	3
3	0.0170594	0.0165376	0.016204	0.0179494	0.0139325	0.0167813	0.0165917	0.01749	0.0181961
								4	
5	0.0380067	0.036827	0.0360731	0.0400228	0.0316332	0.0373727	0.036941	0.03899	0.0406032
α	0.5	1.5	2.5	-0.5	-1.5	0.5	0.5	0.5	0.5
γ	0.5	0.5	0.5	0.5	0.5	1.5	2.5	-0.5	-1.5

Nu (TABLE 7)

M	I	II	III	IV	V	VI	VII	VIII	IX
1	1.02339	1.40471	1.71219	0.488646	-1.17998	1.01972	1.01718	1.02884	1.03647
3	1.02244	1.40409	1.71173	0.486794	-1.1797	1.01878	1.01625	1.02789	1.03551
5	1.02088	1.40307	1.71097	0.483708	-1.17954	1.01722	1.0147	1.02631	1.03391
α	0.5	1.5	2.5	-0.5	-1.5	0.5	0.5	0.5	0.5
γ	0.5	0.5	0.5	0.5	0.5	1.5	2.5	-0.5	-1.5

Sh (TABLE 8)

M	I	II	III	IV	V	VI	VII	VIII	IX
1	0.77875	0.362969	0.017562	1.33188	2.86894	1.28765	1.6883	0.0641607	-1.09204
3	0.778278	0.362129	0.0165221	1.33229	2.86912	1.28751	1.68827	0.0627046	-1.09651
5	0.777487	0.360727	0.0147862	1.33297	2.86928	1.28726	1.68823	0.0602646	-1.104123
α	0.5	1.5	2.5	-0.5	-1.5	0.5	0.5	0.5	0.5
γ	0.5	0.5	0.5	0.5	0.5	1.5	2.5	-0.5	-1.5

τ_x (TABLE 9)

M	I	II	III	IV	V	VI	VII	VIII	IX
1	4.42984	4.46307	4.52686	4.46714	4.48601	5.04772	5.60922	4.47345	4.517
3	4.41336	4.44657	4.51031	4.45167	4.47109	5.03004	5.59044	4.45697	4.5002
5	4.38594	4.41912	4.48277	4.42591	4.44621	5.0006	5.5592	4.42956	4.47311
Q1	0.05	0.15	0.3	0.05	0.05				
Ec	0.01	0.01	0.01	0.05	0.07	So=1.5	2.5	Gm=0.03	0.05

τ_z (TABLE 10)

M	I	II	III	IV	V	VI	VII	VIII	IX
1	0.004290	0.0043115	0.004351	0.0043172	0.0043305	0.0045363	0.0047226	0.0042953	0.0043004
	3	6	6	3	9	5	5	8	2
3	0.017059	0.0171447	0.017305	0.0171694	0.0172241	0.0180484	0.0187974	0.0170798	0.0171001
	4		2						
5	0.038006	0.0381992	0.038562	0.0382629	0.0383905	0.0402491	0.0419478	0.0380531	0.0380993
	7								
Q	0.05	0.15	0.3	0.05	0.05				
1									
Ec	0.01	0.01	0.01	0.05	0.07	So=1.5	2.5	Gm0.03	0.05

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Nu (TABLE 11)

M	I	II	III	IV	V	VI	VII	VIII	IX
1	1.02339	0.974659	0.880292	0.943364	0.902247	1.03561	1.04272	1.02391	1.02442
3	1.02244	0.97367	0.879222	0.941362	0.899662	1.03461	1.04168	1.02296	1.02348
5	1.02088	0.97202	0.877443	0.93805	0.895388	1.03295	1.03994	1.0214	1.02191
Q1	0.05	0.15	0.3	0.05	0.05				
Ec	0.01	0.01	0.01	0.05	0.07	So=1.5	2.5	Gm=0.03	0.05

Sh (TABLE 12)

M	I	II	III	IV	V	VI	VII	VIII	IX
1	0.77875	0.830201	0.929689	0.870561	0.917735	-0.318698	-1.3749	0.779779	0.780808
3	0.778278	0.829778	0.929352	0.871051	0.918759	-0.318252	-1.37342	0.779309	0.780339
5	0.777487	0.829068	0.928786	0.871844	0.920434	-0.317521	-1.37099	0.77852	0.779553
Q1	0.05	0.15	0.3	0.05	0.05				
Ec	0.01	0.01	0.01	0.05	0.07(gm=0.01)	So=1.5	2.5	Gm=0.03	0.05

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